

1 計 算 (1)

p2

確認

$$-4 \quad -8 \quad -64 \quad 1$$

解説

$$\begin{aligned} -2^2 &= -2 \times 2 = -4 \\ (-2)^2 &= (-2) \times (-2) \times (-2) = -8 \\ -4^2 &= -4 \times 4 \times 4 = -64 \\ (-1)^4 &= (-1) \times (-1) \times (-1) \times (-1) = 1 \end{aligned}$$

確認

$$26 \quad -11 \quad 26 \\ -4 \quad -19 \quad -26$$

解説

$$\begin{aligned} -2 \times (-5) + 16 &= 10 + 16 = 26 \\ -21 \div (+7) + (-8) &= -3 - 8 = -11 \\ 20 - 12 \div (-2) &= 20 + 6 = 26 \\ -16 + (-4) \times (-3) &= -16 + 12 = -4 \\ -15 \div (+2) \times 8 &= -3 \cdot 16 = -19 \\ (-4) \times 6 - (-10) \div (-5) &= -24 - 2 = -26 \end{aligned}$$

p3

確認

$$-4ab \quad 6x \\ -\frac{4}{9m} \quad -8xy$$

$$\frac{1}{2m} \quad \frac{3y^4}{2x}$$

解説

$$\begin{aligned} 18ab \times (-2ab) \div 9ab &= -15xy \div 5xy \times (-2x) \\ = -\frac{18ab \times 2ab}{9ab} &= \frac{15xy \times 2x}{5xy} \\ = -4ab &= 6x \\ 8mn \div (-3m) \div 6mn &= 6xy \div 3xy \times (-4xy) \\ = -\frac{8mn}{3m \times 6mn} &= -\frac{6xy \times 4xy}{3xy} \\ = -\frac{4}{9m} &= -8xy \\ -9n^2 r^2 \div (-6mr^4) \div 3m^2 n &= 2xy \times (-3y)^3 \div (6x)^2 \\ = \frac{9m^2 r^2}{6mn^2 \times 3m^2 n} &= -2xy \times (-27y^3) \div 36x^2 \\ = \frac{1}{2m} &= \frac{2xy \times 27y^3}{36x^2} = \frac{3y^4}{2x} \end{aligned}$$

p4

確認

$$-24a^3 \quad \frac{3mn^2}{5}$$

$$-\frac{2y^2}{x} \quad -\frac{12a^2}{b}$$

解説

$$\begin{aligned} 15a^2 x \div \left(-\frac{5}{8}ax\right) \times (-a)^2 &= \frac{9}{10} m^2 n \times 4n \div 6m^2 \\ = -15a^2 x \times \frac{8}{5ax} \times a^2 &= \frac{9}{10} m^2 n \times 4n \times \frac{1}{6m^2} \\ = -24a^3 &= \frac{3mn^2}{5} \\ 6x^2 y^3 \div (2x)^2 \div \left(-\frac{3}{4}xy\right) &= -\frac{2}{3} ab^3 \times 3a \div \frac{1}{6} b^4 \\ = -6x^2 y^3 \times \frac{1}{4x^2} \times \frac{4}{3xy} &= -\frac{2}{3} ab^3 \times 3a \times \frac{6}{b^4} \\ = -\frac{2y^2}{x} &= -\frac{12a^2}{b} \end{aligned}$$

p5

確認

$$\frac{11x+12y}{20} \quad -\frac{11x+7y}{6} \\ -\frac{x+3y}{15} \quad \frac{3x-y}{3}$$

解説

$$\begin{aligned} \frac{3x+4y}{4} + \frac{-x-2y}{5} &= \frac{2x-y}{3} - \frac{5x-3y}{2} \\ = \frac{15x+20y}{20} + \frac{-4x-8y}{20} &= \frac{4x-2y}{6} - \frac{15x-9y}{6} \\ = \frac{11x+12y}{20} &= \frac{-11x+7y}{6} \\ \frac{x+7y}{10} - \frac{x+3y}{6} &= 2x+y - \frac{3x+4y}{3} \\ = \frac{3x+21y}{30} - \frac{5x+15y}{30} &= \frac{6x+3y}{3} - \frac{3x+4y}{3} \\ = \frac{-2x+6y}{30} &= \frac{3x-y}{3} \\ = -\frac{x+3y}{15} \end{aligned}$$

p6

確認

$$x=3 \quad x=\frac{3}{4} \quad x=\frac{3}{16} \quad x=-\frac{25}{3}$$

解説

$$\begin{aligned} 0.3x + 0.4 &= 0.1x + 1 \text{ の両辺を10倍して} \\ 10(0.3x + 0.4) &= 10(0.1x + 1) \\ 3x + 4 &= x + 10 \text{ より} \\ 2x - \frac{5}{4} &= \frac{x}{3} \text{ の両辺を12倍して} \\ 12\left(2x - \frac{5}{4}\right) &= 12 \times \frac{x}{3} \\ 24x - 15 &= 4x \text{ より} \\ \frac{4x-5}{2} - \frac{2x-9}{3} &= \frac{3}{4} \text{ の両辺を12倍して} \\ 12\left(\frac{4x-5}{2} - \frac{2x-9}{3}\right) &= 12 \times \frac{3}{4} \\ 6(4x-5) - 4(2x-9) &= 9 \text{ より} \\ x + 3 - \frac{x-4}{2} &= \frac{5}{6} \text{ の両辺を6倍して} \\ 6\left(x + 3 - \frac{x-4}{2}\right) &= 6 \times \frac{5}{6} \\ 6x + 18 - 3(x-4) &= 5 \text{ より} \end{aligned}$$

p7

確認

$$x=6 \quad x=0 \quad x=\frac{2}{3} \quad x=-\frac{15}{28}$$

解説

$$\begin{aligned} 0.2(x-5) - 1.2(x-3) &= -3.4 \text{ の両辺を10倍して} \\ 2(x-5) - 12(x-3) &= -34 \text{ より} \\ \frac{1}{4}(5x-2) - \frac{3}{2}(2x-3) &= 4 \text{ の両辺を4倍して} \\ (5x-2) - 6(2x-3) &= 16 \text{ より} \\ 2(3x-2) = 0.3(-x+4) - 1 \text{ の両辺を10倍して} \\ 20(3x-2) = 3(-x+4) - 10 \text{ より} \\ \frac{2}{3}(-x-3) + \frac{3}{4}(4x+5) &= \frac{1}{2} \text{ の両辺を12倍して} \\ 12 \times \frac{2}{3}(-x-3) + 12 \times \frac{3}{4}(4x+5) &= 12 \times \frac{1}{2} \\ 8(-x-3) + 9(4x+5) &= 6 \text{ より} \end{aligned}$$

p8

確認

$$x = 1, y = 3 \quad x = 6, y = -1$$

解説

$$\begin{cases} 3x + 1 = 2(y - 1) \cdots \\ -7x - (5 - 3y) = -3 \cdots \end{cases}$$

よじり $3x - 2y = -3 \cdots$
よじり $-7x + 3y = 2 \cdots$
 $\times 3 + \times 2$
 $9x - 6y = -9$
 $+$ $-14x + 6y = 4$
 $-5x = -5$
 $x = 1$

$$\begin{aligned} x = 1 \text{ を 代入} \\ 3 \times 1 - 2y = -3 \\ -2y = -6 \\ y = 3 \end{aligned}$$

$$\begin{cases} \frac{1}{4}x + \frac{1}{2}y = 1 \cdots \\ \frac{1}{3}x - \frac{1}{4}y = \frac{9}{4} \cdots \end{cases}$$

$\times 4$ より $x + 2y = 4 \cdots$
 $\times 12$ より $4x - 3y = 27 \cdots$
 $\times 3 + \times 2$
 $3x + 6y = 12$
 $+$ $8x - 3y = 54$
 $11x = 66$
 $x = 6$

$$\begin{aligned} x = 6 \text{ を 代入} \\ 6 + 2y = 4 \\ 2y = -2 \\ y = -1 \end{aligned}$$

p9

確認

$$y = -\frac{2x}{5} - \frac{12}{5} \quad a = -b + 3$$

$$y = \frac{x}{2} + 2 \quad a = b + \frac{3y}{2}$$

解説

$$\begin{cases} 2x + 5y = -12 \quad [y] \\ 5y = -2x - 12 \\ y = -\frac{2x}{5} - \frac{12}{5} \end{cases} \quad \begin{cases} 12 = 4(a + b) \quad [a] \\ 12 = 4a + 4b \\ 4a = 4b - 12 \\ a = -b + 3 \end{cases}$$

$$\begin{cases} \frac{x}{4} - \frac{y}{2} = -1 \quad [y] \\ \frac{x}{4} - \frac{y}{2} = -1 \\ \text{両辺を4倍して} \\ x - 2y = -4 \\ -2y = -x - 4 \\ y = \frac{x}{2} + 2 \end{cases} \quad \begin{cases} y = \frac{2}{3}(a - b) \quad [a] \\ y = \frac{2}{3}(a - b) \\ \text{両辺を3倍して} \\ 3y = 2(a - b) \\ 3y = 2a - 2b \\ -2a = -2b - 3y \\ a = b + \frac{3y}{2} \end{cases}$$

p10

$$\begin{aligned} 1 \quad & 32 \quad -\frac{1}{2} \\ & \frac{2}{7} \quad 6 \\ & -8 \quad -\frac{1}{5} \end{aligned}$$

解説

$$\begin{aligned} (-6)^2 + \frac{1}{2} \times (-8) &= 36 - 4 = 32 \\ \left(\frac{1}{4} - \frac{2}{3}\right) \div \frac{5}{6} &= -\frac{5}{12} \times \frac{6}{5} = -\frac{1}{2} \\ \left(-\frac{9}{14}\right) \div \frac{3}{8} + 2 &= -\frac{9}{14} \times \frac{8}{3} + 2 = -\frac{12}{7} + 2 = \frac{2}{7} \\ (-4)^2 + 5 \times (-2) &= 16 - 10 = 6 \\ (-2)^2 - 4 \times 3 &= 4 - 12 = -8 \\ -\frac{3}{7} \times \left(\frac{4}{5} - \frac{1}{3}\right) &= -\frac{3}{7} \times \frac{7}{15} = -\frac{1}{5} \end{aligned}$$

2 $-30a^3$

$\frac{2a^2}{b}$

$2a^2b$

$-3ab^2$

$8a^2b$

$-6a^2b^2$

解説

$$\begin{aligned} (-2a) \div (-4ab) &= 6ab^2 \times 4a \div 3b \\ = -8a^2 \div (-4ab) &= \frac{6ab^2 \times 4a}{3b} \\ = \frac{8a^3}{4ab} &= 8a^2b \\ = \frac{2a^2}{b} & \\ 3a^2 \div 6ab \times 4ab^2 &= 12a^2b \div (-6ab) \times 3ab^2 \\ = \frac{3a^2 \times 4ab^2}{6ab} &= -\frac{12a^2b \times 3ab^2}{6ab} \\ = 2a^2b &= -6a^2b^2 \end{aligned}$$

p11

3 $8x - 5y$

$\frac{7a-b}{6}$

$-4a + 9b$

$\frac{x+1}{6}$

解説

$$\begin{aligned} 3(2x - 3y) + 2(x + 2y) &= 4(a + b) - (8a - 5b) \\ = 6x - 9y + 2x + 4y &= 4a + 4b - 8a + 5b \\ = 8x - 5y &= -4a + 9b \\ \frac{3a+b}{2} - \frac{a+2b}{3} &= \frac{4x-5}{6} - \frac{x-2}{2} \\ = \frac{9a+3b}{6} - \frac{2a+4b}{6} &= \frac{4x-5}{6} - \frac{3x-6}{6} \\ = \frac{7a-b}{6} &= \frac{x+1}{6} \end{aligned}$$

4 $x = -5$

$x = -6$

5 $x = -3, y = 2$

p12

$x = 1, y = -1$

6 $x = -\frac{2y}{3} + 4$

$a = -b + \frac{1}{2}$

$x = -1$

$x = -3$

$x = 3, y = -5$

$x = 2, y = 4$

$b = -\frac{3a}{2} + \frac{5}{2}$

$b = 2m - a$

解説

$$\begin{aligned} 3x + 2y = 12 \quad [x] & \quad 3a + 2b = 5 \quad [b] \\ 3x = -2y + 12 & \quad 2b = -3a + 5 \\ x = -\frac{2y}{3} + 4 & \quad b = -\frac{3a}{2} + \frac{5}{2} \end{aligned}$$

$l = 2(a + b) \quad [a]$

$l = 2a + 2b$

$-2a = 2b - l$

$a = -b + \frac{l}{2}$

$m = \frac{1}{2}(a + b) \quad [b]$

$2m = a + b$

$2m = a + b$

$-b = -2m + a$

$b = 2m - a$